

# ZEEMAN EFFECT FOR ONE ELECTRON

Paschenbach effect <sup>Weak magnetic field</sup> Strong

## Normal Zeeman Effect (2) Anomalous Zeeman Effect

The effect of magnetic field on the spectrum is called Zeeman effect. It was observed that a single spectral line splits up into three components such that one line has got a larger frequency, other a lower frequency than the frequency of original line and third one has the frequency of original line. This was named as normal Zeeman effect.

But later on much more complicated splitting was observed and was called anomalous Zeeman effect.

### Vector model of the atom:-

(1) Normal Zeeman effect is produced in the case of a singlet line.

(2) orbital motion of the electron is sufficient to explain this normal Zeeman effect.

(3) Anomalous Zeeman effect is produced by doublet or triplet lines such as (10, 3 etc). This effect can be explained by considering the spin motion besides orbital motion.

When an atom is placed in a magnetic field the electron ~~orbital~~ begins to execute a precessional motion around the direction of the applied magnetic field.



The precessional frequency of [Larmor] is given by the formula  $\omega = \frac{e}{4\pi m e} H$  |  $\omega_L = \frac{e}{2m c} H$

On account of this precessional motion the energy of the electron changes. The change of the magnetic energy

$$\Delta E = \omega_L \cdot l \cdot \frac{h}{2\pi} \cos(\theta, H) \quad \left[ \text{Projection of the precessional vector in the direction of the field} \right]$$

$$\omega = \frac{\omega}{2\pi}$$

$$= \frac{e}{2m c} H \cdot l \cdot \frac{h}{2\pi} \cos(\theta, H)$$

$$= \frac{e h}{2m c 2\pi} H \cdot l \cos(\theta, H)$$

$$\Delta E = \frac{e h}{4\pi m c} H \cdot l \cos(\theta, H)$$

$$\Delta E = \frac{e h}{4\pi m c} H m_l \quad \text{where } m_l = \text{magnetic quantum number}$$

Let  $E_0'$  and  $E_0''$  be the energy of final and initial level in the absence of magnetic field. ①A

Let  $E_H'$  and  $E_H''$  be the corresponding energy in the presence of the field. So

$$E_H' = E_0' + \frac{e\hbar}{4\pi m_e c} H m_l' \quad (2)$$

where  $m_l'$  is the magnetic quantum no. of the final level and  $m_l''$  of the initial level.

$$E_H'' = E_0'' + \frac{e\hbar}{4\pi m_e c} H m_l'' \quad (3)$$

When transition occurs from higher energy levels to lower energy levels then

$$h\nu = E_H'' - E_H' \quad (3-2)$$

$$= (E_0'' - E_0') + \frac{e\hbar}{4\pi m_e c} H (m_l'' - m_l') \quad \frac{\nu}{c} = \lambda = \bar{\nu} = \text{wave no.}$$

$\frac{1}{\lambda} = \frac{1}{\lambda_0} + \Delta \frac{1}{\lambda}$

$$h\nu = h\nu_0 + \frac{e\hbar}{4\pi m_e c} H \Delta m_l$$

$$\nu = \nu_0 + \frac{e\hbar}{4\pi m_e c} H \Delta m_l \quad (4)$$

where  $\frac{e\hbar}{4\pi m_e c} = L$  called the Landé g-factor and represents the normal Zeeman effect.

① then  $\nu = \nu_0$

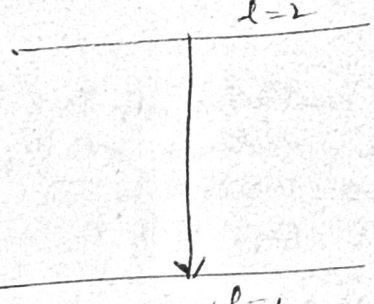
② when  $\Delta m_l = -1$

$$\nu = \nu_0 - \frac{e\hbar}{4\pi m_e c} H$$

③ when  $\Delta m_l = +1$

$$\nu_H = \nu_0 + \frac{e\hbar}{4\pi m_e c} H$$

Now we consider the normal Zeeman effect of  $l=2$  level with magnetic field.



if  $l=1$  then  $m = -1, 0, 1$   
 if  $l=2$  then  $m = -2, -1, 0, 1, 2$

